

Defining Agents via Strategies: Towards a view of MAS as Games

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September 2005 / WRAC (Nasa)



Extensional x Intentional Models

Some Examples

- Naive Set Theory \times Axiomatic Set Theory
- Computable Functions \times Turing Machines
- Alternative World Views \times Logical Modal Theories
- Behavior/Communication \times Process Calculus Terms
- Models \times Theories

Diff. Intensional Flavors

- Process Calculi Terms × Presentation of Modal Theories
- Automata × Logical Modal Theories
- Reactive Systems × Rewriting Systems
- Reactive Systems × First-Order Logic + Modal Logic
- BDI Agents × LORA Theories

The "Intention \times Extension" relationship in Practice

Consistency and Completeness

- Is there an Extension ??
- Is there an (interesting) Intention ??
- Is the intended extension the right one ???

How to know that in practice ?

- Gödel's theorems show that even for "simple" theories the answer for those questions are strongly related each other and are either negative or unknown.
- In most of the cases it is not possible to know that. (Theory of Science)

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TECMF-DI-Rio: Technology in Formal Methods

The role of The Formal Analysis of Systems/Theories

Provide techniques, tools and methodology to work out the Principle of False-ability of Theories towards the (Formal) validation of software/specification.

Known Techniques/Tools

- Ad-hoc and Systematic Testing.
- Simulation (stochastic).
- Modal Logic and Model-Checking Algorithms.
- Process Calculi, μ -calculus proof-system.
- Theorem Proving.



Game-Theory: From the Quantitative to the Qualitative Approach

In Social and Economic Sciences

- Game Theory has been used as an important Formal (Math) Analysis tool.
- Existence of: Winning Strategies, Nash Equilibria, Subgame Perfect/Imperfect Equilibria, in competitive games, are conceptually meaningful.
- The *core* of a coalition game plays interesting concepts in cooperative environments.



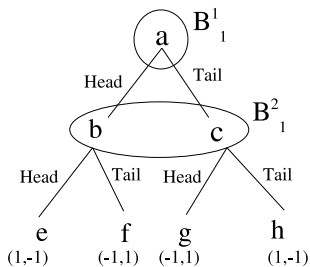
Game-Theory: From the Quantitative to the Qualitative Approach

Why not Model-Checking games ?

Previous work in *ATL*[Alur,Henziger and Kuppelman] and *GAL*[TECMF].



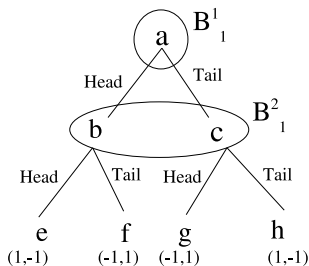
Extensive Games



An extensive game is:

- A Game Tree
- A partition of the nodes among players
- Strategies (for each player)
- Payoffs at terminal nodes.

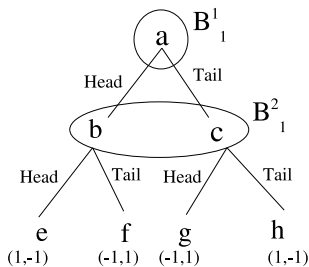
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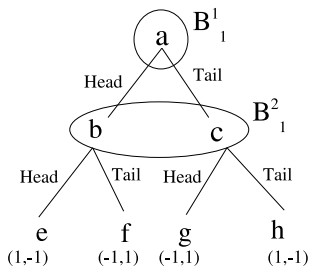
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Games × MAS

MAS validation by means of quantitative based games

- A quite useful tool for auctions formal (math) Analysis.
- Agent-based modeling and Nash Equilibria Analysis in Power Market [KABC2003].
- A Game-Theoretic approach for power aware middleware [MV2005]
- Many more.....



Games × MAS

A Foundational Question

Why can we use game-theoretic tools for MAS validation ???



Our contribution

- Class G of MAS, such that, there is no simultaneous action occurrence from different agents, and, the set of Desires, Intentions and Beliefs of each agent is a finite set of propositions.
- Lemma I: Every MAS belonging to G is, essentially, a Game.
- Lemma II: Every Game can be implemented as a MAS. Equilibria are Optima Desires Satisfaction.

Work-in-Progress

Conjecture: Every BDI based MAS is a Coalition Game with transferable payoff.

Corollary: Agent's rationality = Player's rationality

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The Agent's Individual Behavior

Agent's Control Loop

```
B := B0; I := I0;  
While(true)  
  get next percept  $\rho$ ;  
  B := brf(B,  $\rho$ );  
  D := options(B, I);  
  I := filter(B, D, I);  
   $\pi$  := plan(B, I);  
  execute( $\pi$ );  
end-while;
```

The Planning

A Planning is a partial mapping from Sets of Possible into Sets of Possible Worlds



Agents as Players

Agent Concept	Game Concept
Beliefs	State-Description
Intention	Strategy
Desires	Maximization of Payoffs

The payoff is associated to the number of desires satisfied in a possible behavior of the MAS

Proof-sketch of Lemma 1

- A MAS is identified with its extensional Model M ($\triangleright T$ Kripke Semantics $\triangleright S$).
- Define $s \equiv s'$ in the situation model Sit_M , iff, they are bisimilar and elementarily equivalent.
- Sit_M / \equiv provides the game tree of G_M .
- The source of the actions in Sit_M / \equiv defines the players.
- Strategies of p_a are determined by each action taken by agent a .
- The payoff of a terminal node is the number of desires satisfied at the node, for each agent.
- \implies Subgame Equilibria of G_M will correspond to states with maximal social satisfaction of M .



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Agents as Players: Integrated View

Agency Theory	Game Theory
Agents Groups	Players
Common Beliefs	Game Tree
Agent's Intentions	Player's Strategies
Desires Satisfaction ¹	Existence of Equilibria

¹Here we refer to the satisfaction of desires of a set of agents

Proof-Sketch of Lemma II

- Each agent corresponds to a player.
- The desire of the player is to maximize the payoff.
- Beliefs are state descriptions of the extensive game.
- The strategies of each player determines the Planning of the each agent.
- \implies States of maximal social of M (if any) are subgame perfect equilibria of the game.

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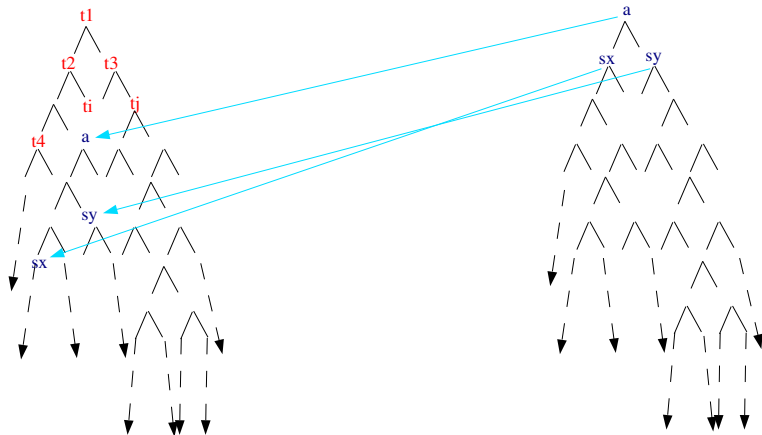
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Time is important in BDI Agents

Return

Temporal Structures and Substructures



The Situation Semantics

Return

